

# How to Estimate Motor Driver Power Dissipation

MPS Jackson Gao

# Half-Bridge Power Losses: 1st Order Estimation

## MOSFET Turn-On Losses

$$P_D = \frac{V_{IN}}{2} \times I_{MOTOR} \times \frac{t_{RISE}}{T_{PWM}}$$

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$$P_D = \frac{V_{IN}}{2} \times I_{MOTOR} \times \frac{t_{FALL}}{T_{PWM}}$$

$t_{RISE} = t_{FALL}$  (VDS transition)

## MOSFET Switching Losses

$$P_{SW} = V_{IN}^2 \times I_{MOTOR} \times f_{PWM} \times \frac{1}{SR}$$

Where  $I_{MOTOR}$  is assumed to have a very low ripple

## MOSFET Conduction Losses

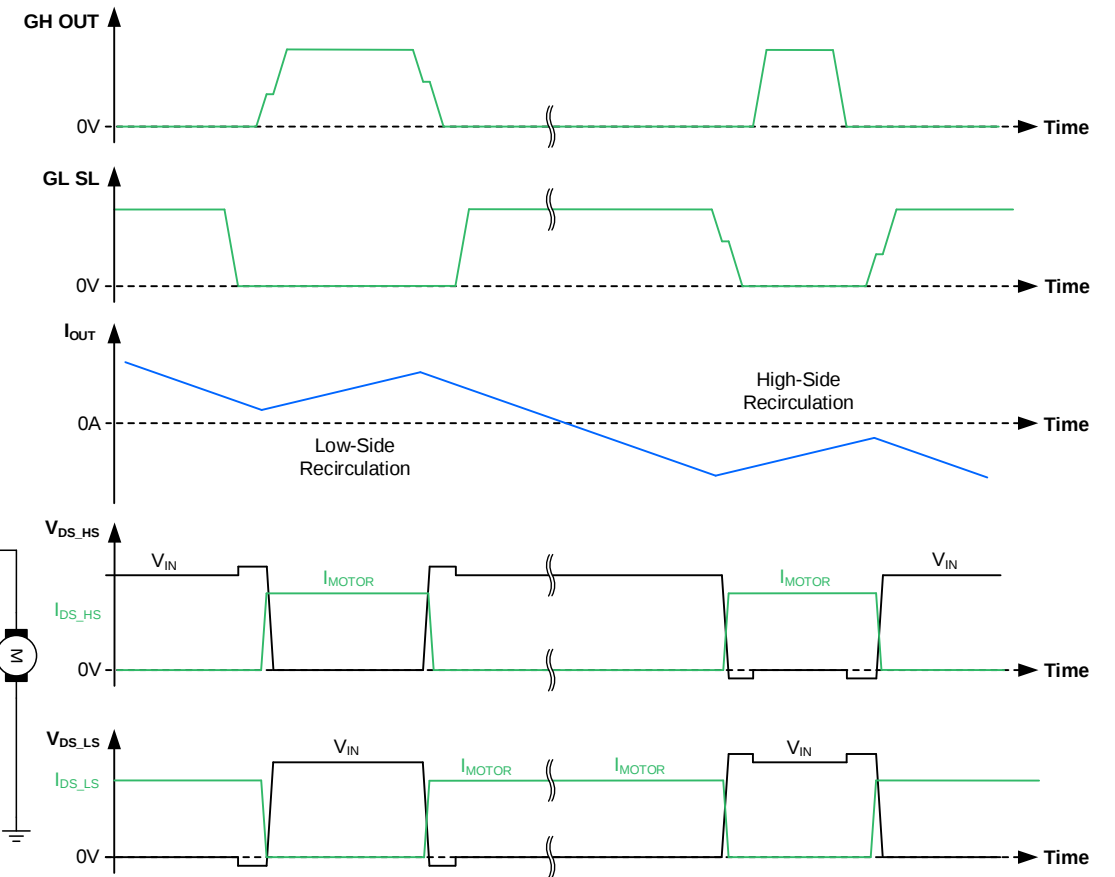
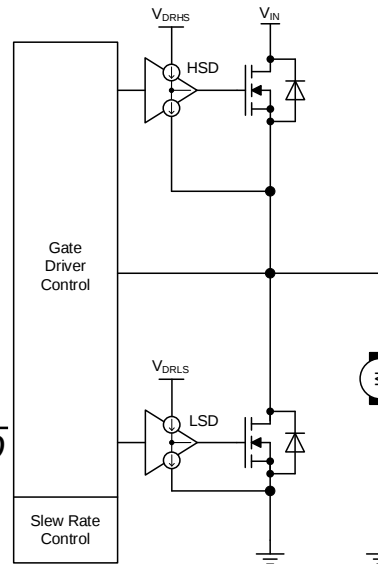
$$P_{COND} = R_{DS(ON)} \times I^2_{(RMS)} \quad I_{RMS} = I_{MOTOR} \times \sqrt{D}$$

$$P_{COND} = R_{DS(ON)} \times I^2_{MOTOR} \times D$$

## MOSFET Back-Gate Diode Losses

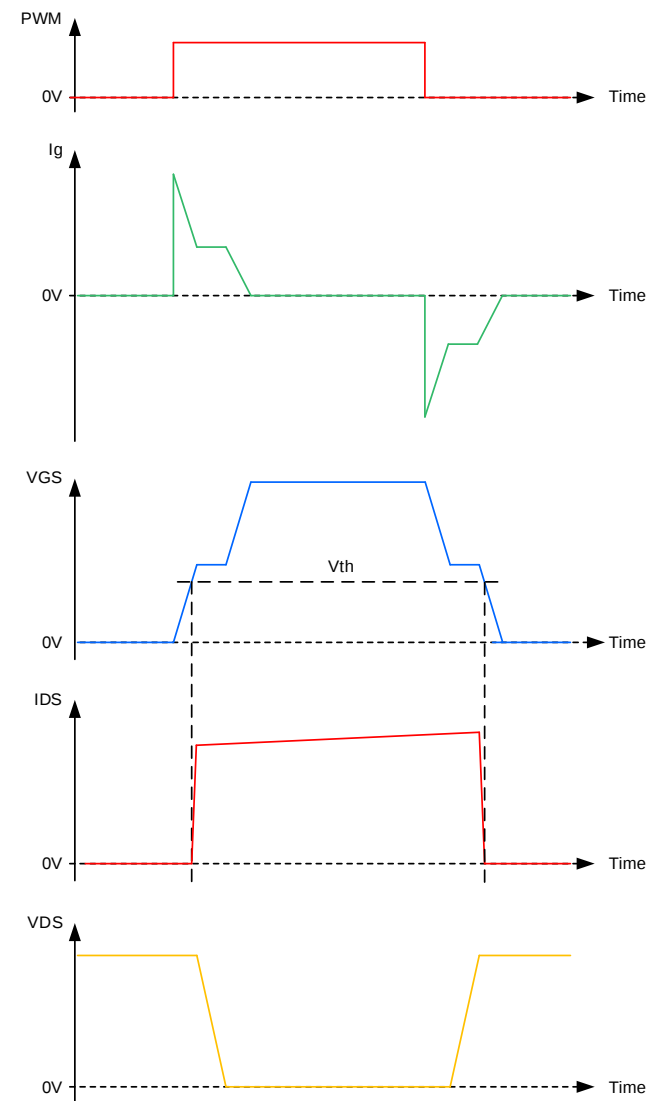
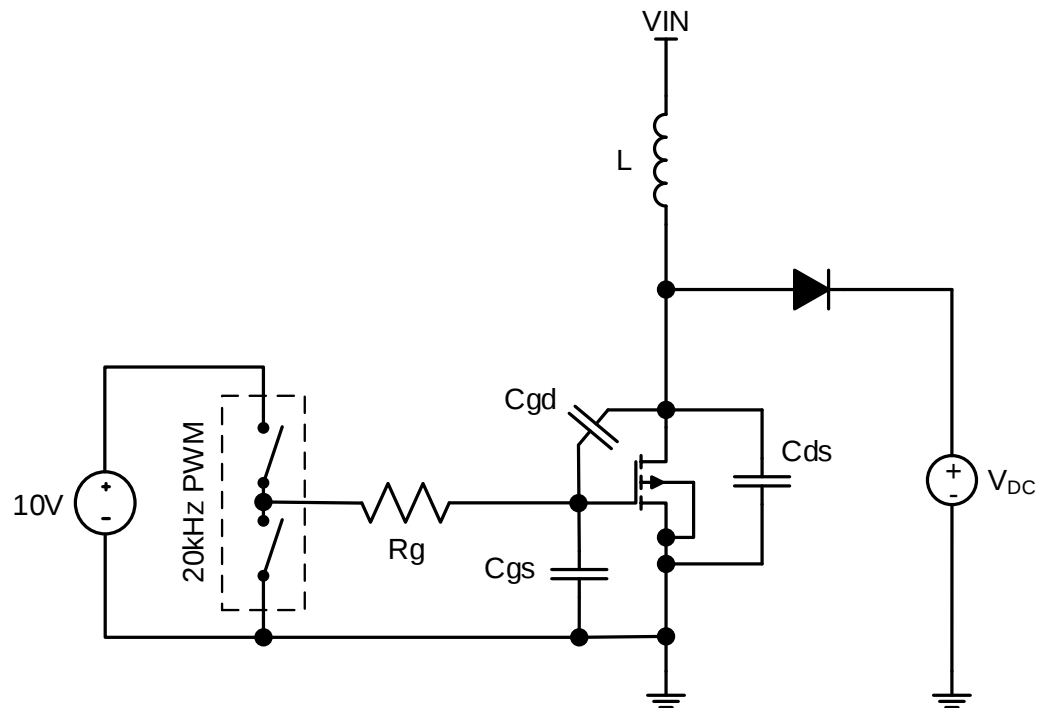
$$P_{BG} = 2 \times V_F \times I_{MOTOR} \times t_{BG\_TIME} \times f_{PWM}$$

Where the  $I_{DS}$  transition is assumed to be negligible

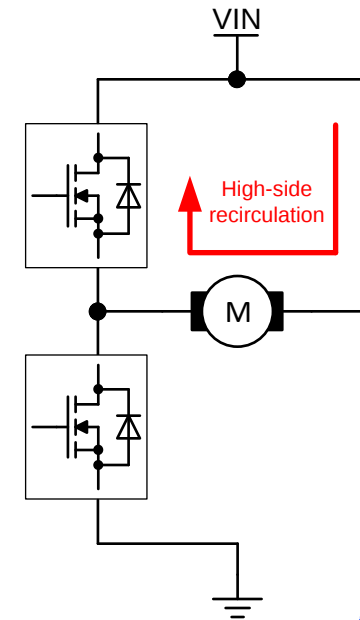
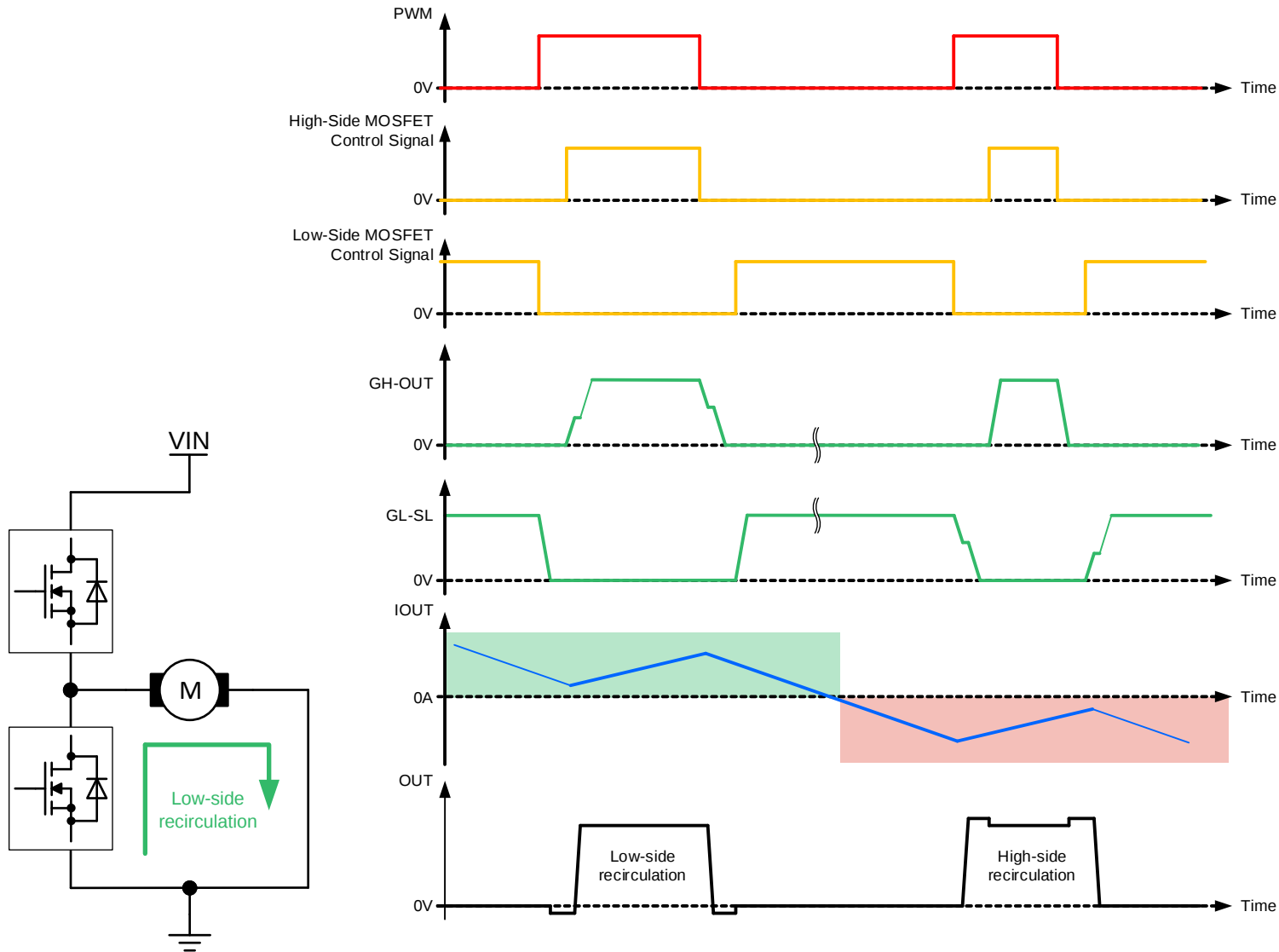


# Understanding MOSFET Basic Switching (Inductive Load)

|                              |           |                                                               |      |    |
|------------------------------|-----------|---------------------------------------------------------------|------|----|
| Input Capacitance            | $C_{iss}$ | $V_{DS} = 15\text{ V}, V_{GS} = 0\text{ V}, f = 1\text{ MHz}$ | 5861 | pF |
| Output Capacitance           | $C_{oss}$ |                                                               | 224  |    |
| Reverse Transfer Capacitance | $C_{rss}$ |                                                               | 185  |    |



# Half-Bridge Switching Waveforms



# Half-Bridge Power Losses: 1st Order Estimation

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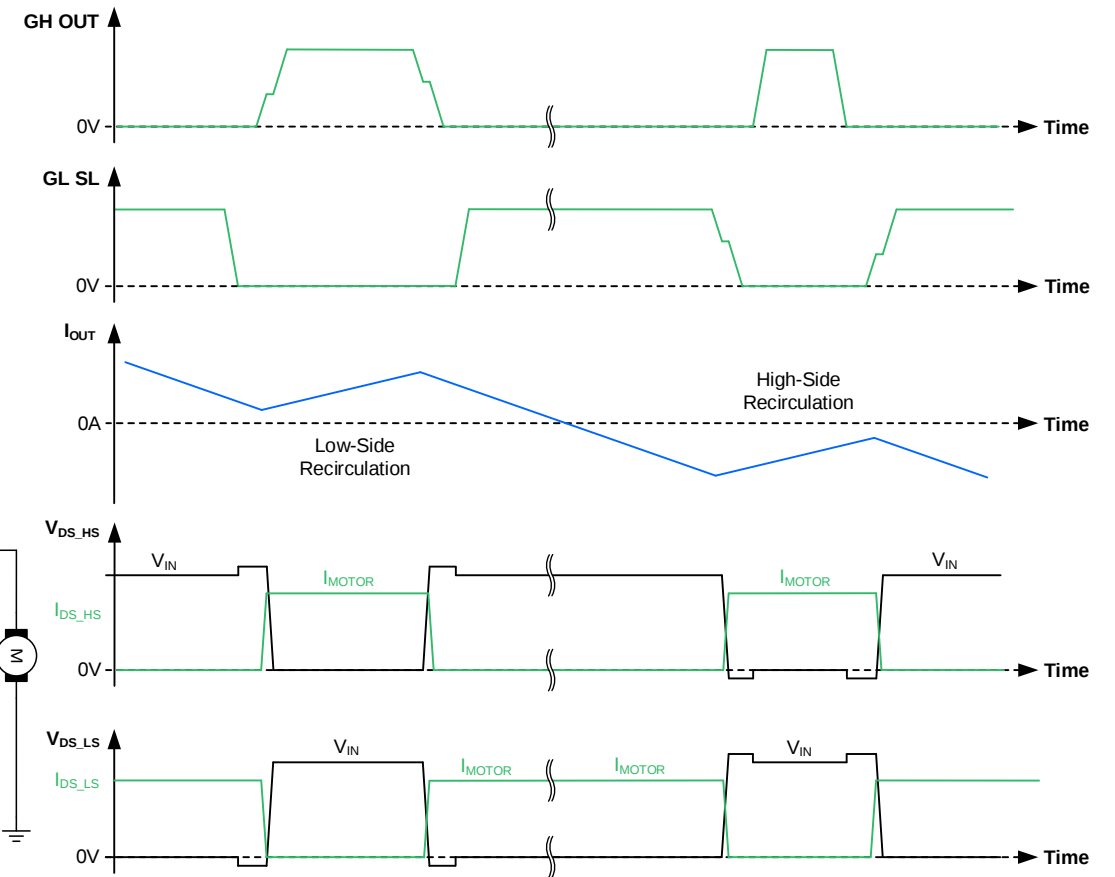
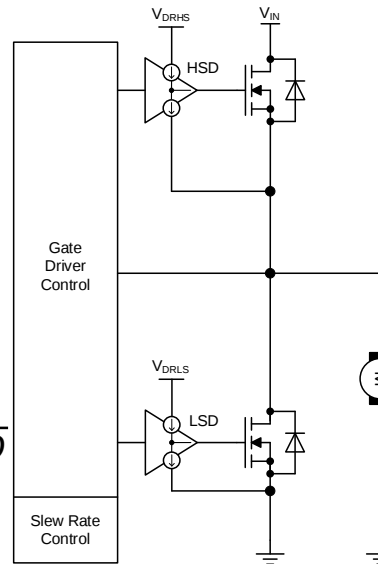
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## MOSFET Back-Gate Diode Losses

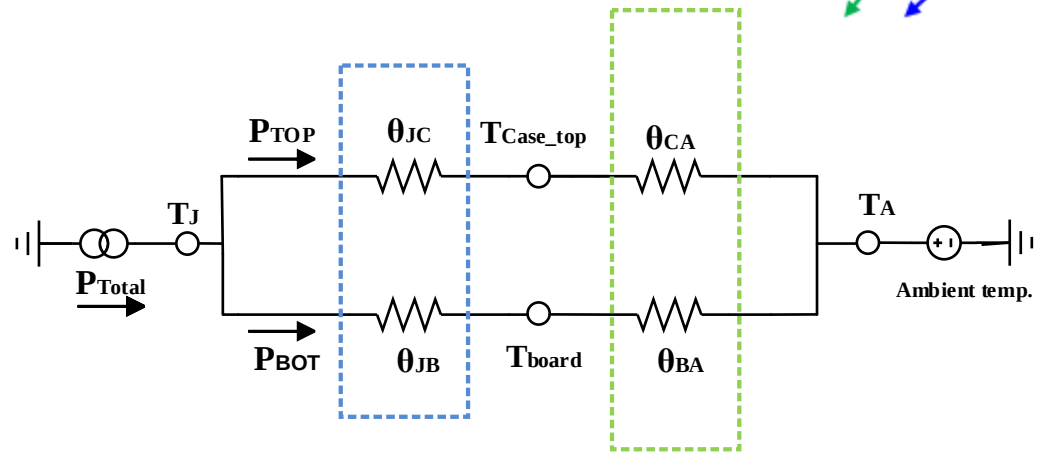
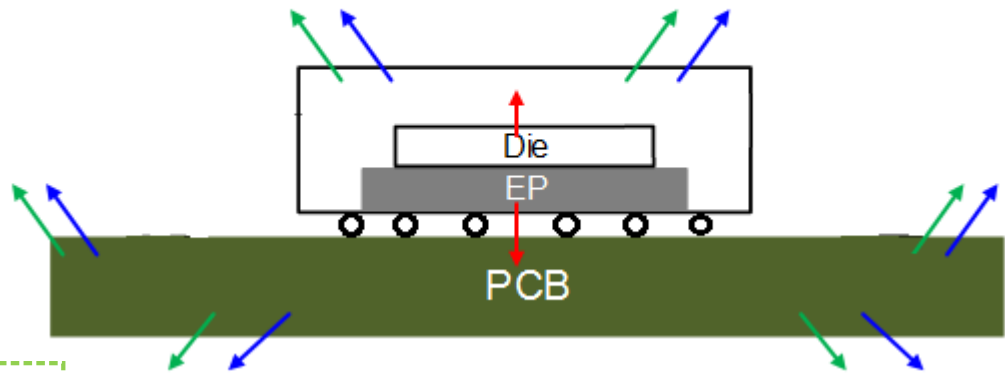
$$P_{BG} = 2 \times V_F \times I_{MOTOR} \times t_{BG\_TIME} \times f_{PWM}$$

Where the  $I_{DS}$  transition is assumed to be negligible



# Steady State Thermal Modeling

Heat Transfer Paths



  Package specific

  Not part of package

$$R_{Jx} \text{ or } \theta_{Jx} = \frac{T_J - T_x}{P_{Jx}}$$

$$\Psi_{Jx} = \frac{T_J - T_x}{P_{total}}$$

$$\theta_{JA} \quad \Psi_{JT} \quad \Psi_{JB}$$

$\theta_{jx}$ =junction-to-x thermal resistance

$T_j$ =junction temperature

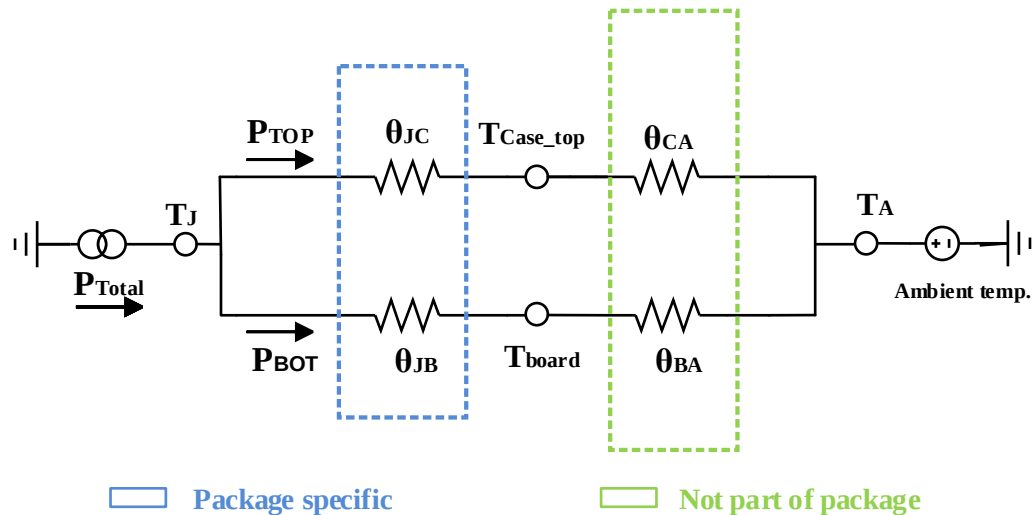
$T_x$ =the specific point temperature

$P_{jx}$ =the power loss of heat flow through x

$P_{total}$ =the total power

For natural convection heat transfer,  
>90% of the heat is dissipated by the board and not from the package surfaces

# How To Use Thermal Resistance Parameters



- $\Psi_{JB}$ : Characteristic thermal resistance allowing system designers to calculate the device’s junction temperature based on a board temperature measurement. The  $\Psi_{JB}$  metric should be close to  $\theta_{JB}$ , as the PCB dissipates most of the heat of the device.

$$T_J = \textcolor{red}{T_{PCB}} + (\Psi_{JB} \times P_D)$$

- $\Psi_{JT}$ : Characteristic thermal resistance reflecting the temperature difference between the die (junction) and the top of the package.  $\Psi_{JT}$  is not a true thermal resistance, as the heat flowing from the die to the top of the package is unknown (but assumed to be the total power of the device). This assumption is clearly not valid, but when calculated this way,  $\Psi_{JT}$  becomes a very useful number as its characteristics are much like the application environment of the IC package.

$$\Psi_{JT} = \frac{T_J - T_C}{P_D}$$

$$T_J = \textcolor{red}{T_{case}} + (\Psi_{JT} \times P_D)$$

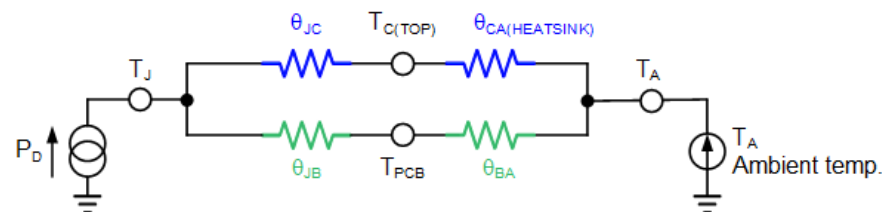
## Thermal Metrics <sup>(4)</sup>

|                                                      |          |
|------------------------------------------------------|----------|
| $\theta_{JA}$ (junction-to-ambient).....             | 44.3°C/W |
| $\theta_{JC\_TOP}$ (junction-to-case top).....       | 37.5°C/W |
| $\theta_{JC\_BOTTOM}$ (junction-to-case bottom)..... | 2.6°C/W  |
| $\theta_{JB}$ (junction-to-board).....               | 5.3°C/W  |
| $\Psi_{JT}$ (junction-to-top).....                   | 1.1°C/W  |
| $\Psi_{JB}$ (junction-to-board).....                 | 5.1°C/W  |

Notes:

# Pulsed Operation

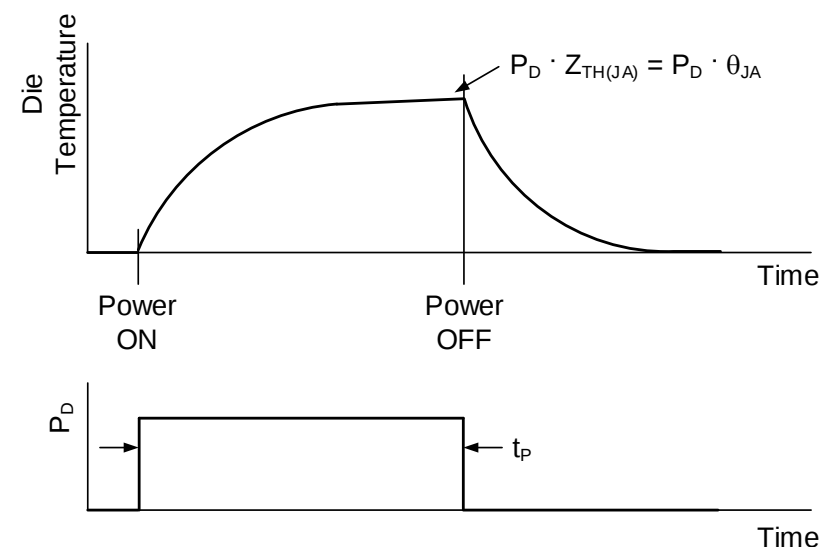
Under pulsed load operation, higher peak power dissipation can be tolerable. The critical junction temperature is not reached instantaneously, even when excessive power is being dissipated in the device.



$\theta_{JB}$ : Thermal impedance from the die to the board.  $\theta_{JB}$  includes some of the board characteristics and their coupling with the package.

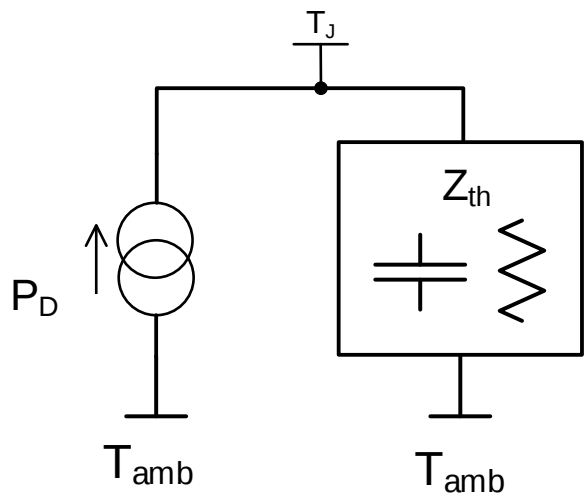
Thermal capacitance ( $C_{TH}$ ) is a measure of the capability to accumulate heat and it depends on the specific heat capacity ( $c$ ), volume ( $V$ ), and density ( $\rho$ ):

$$C_{TH} = c \cdot \rho \cdot V \quad \text{expressed in J/K}$$



# Transient Thermal Modeling

Any  $Z_{th}(s)$  impedance can be synthesized in a passive network using the Cauer or Foster algorithm. For thermal models, RC networks result quite handy and representative of the reality.

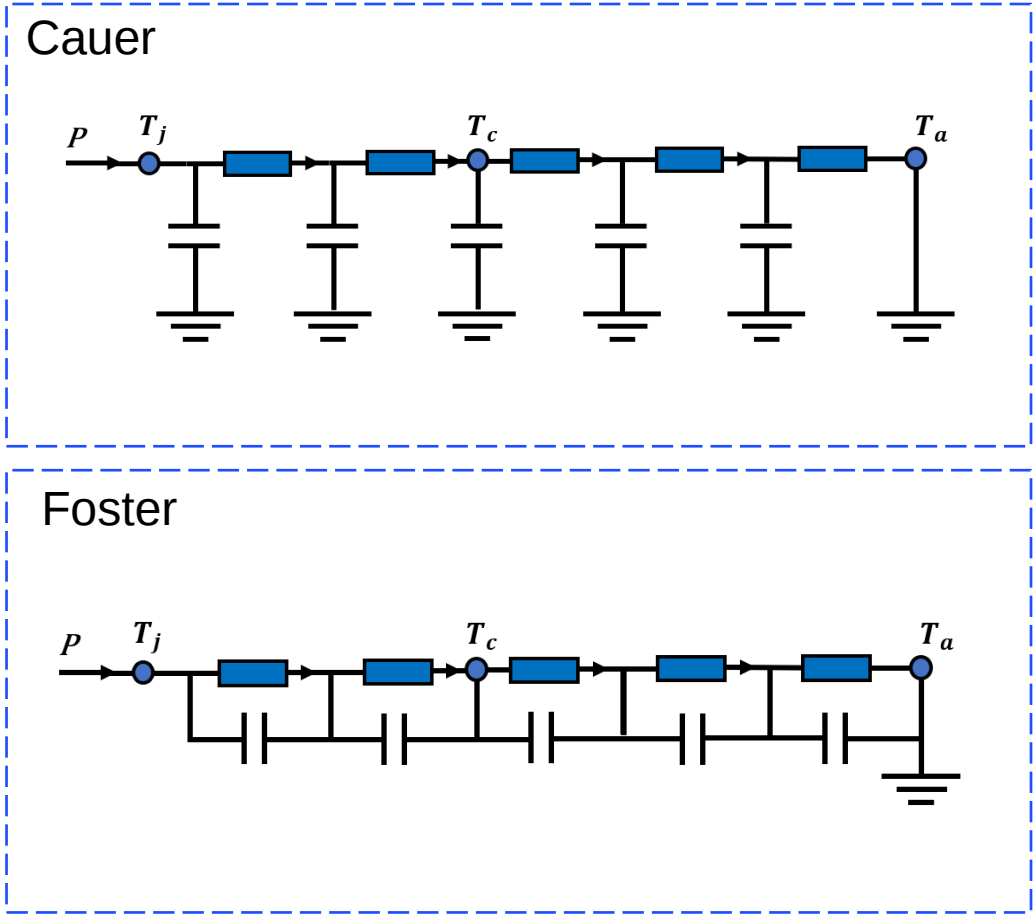


$$Z_{th}(s) = \frac{N_{th}(s)}{D_{th}(s)}$$

RC network extraction from  $Z_{th}(s)$ :  
Cauer or Foster representation

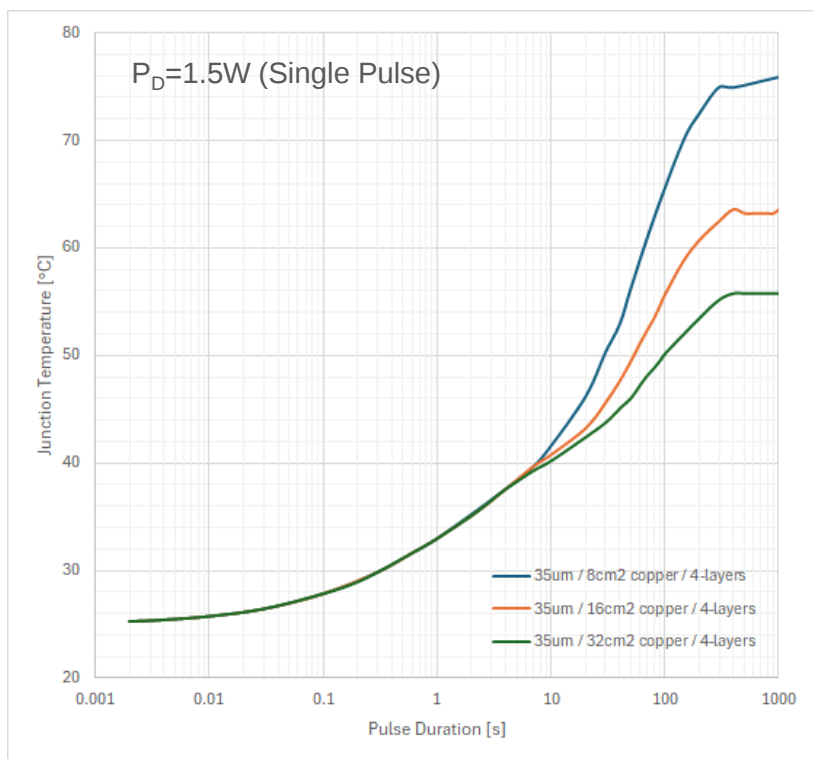
$$Z_{th}(t) = \sum_{i=1}^n r_i \left( 1 - e^{-\frac{t}{\tau_i}} \right)$$

$$\tau_i = r_i c_i$$



# Transient Thermal Modeling(Cont'd)

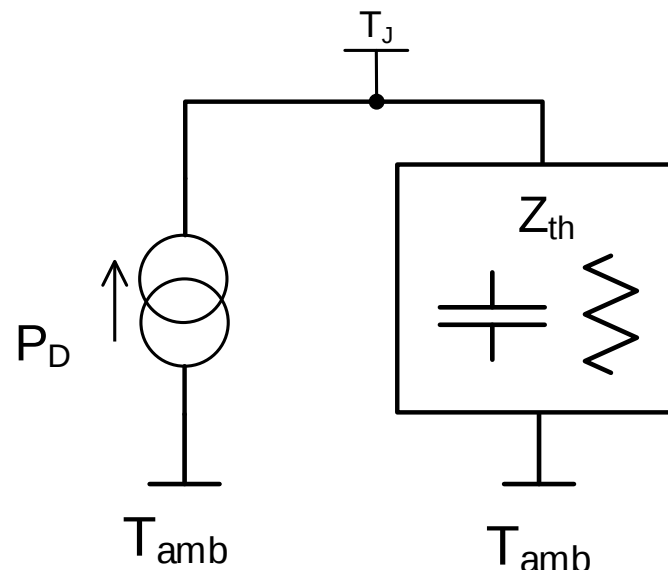
## Transient Measurements



$$T_j(t) = T_J(0) + f(t)$$

$T_j(t)$  can be found using curve fitting techniques

## Model



$$T_j(t) = \underbrace{T_{amb}}_{T(0)} + \underbrace{PD(t) * Zth(t)}_{f(t)}$$

$\mathcal{L} \downarrow$

$$\mathcal{L}\{T_j(t) - T_J(0)\} = PD(s) Zth(s)$$



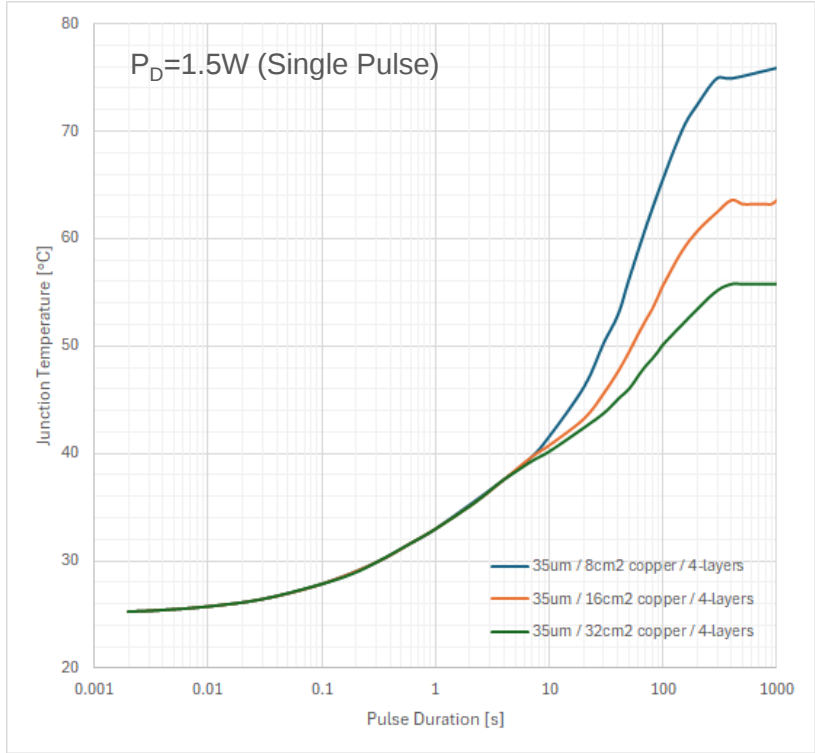
$$Z_{th}(s) = \frac{\mathcal{L}\{T_j(t) - T_J(0)\}}{P_D(s)}$$

To know  $Z_{th}(s)$  one needs:

- $T_j(t)$  time response (i.e. to step or impulse power dissipation stimuli)
- resting condition  $T_J(0)$  (temp. when no power dissipation is applied)
- stimuli function (i.e. step or impulse and its amplitude)

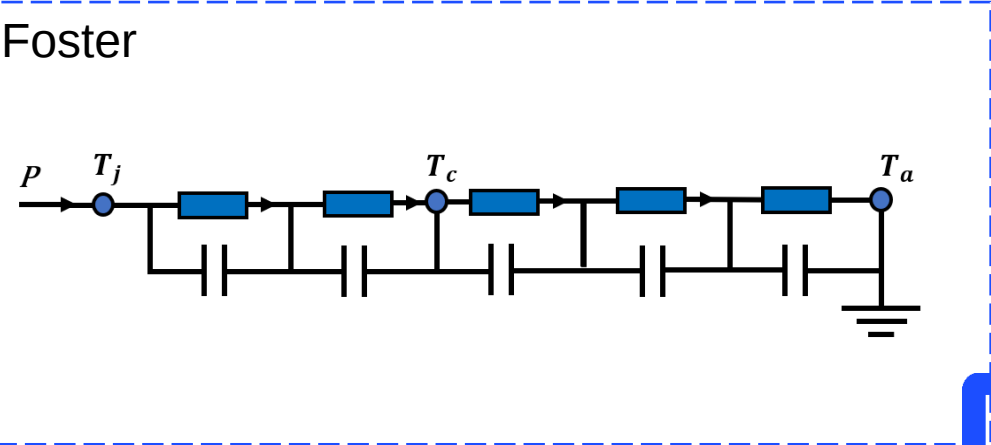
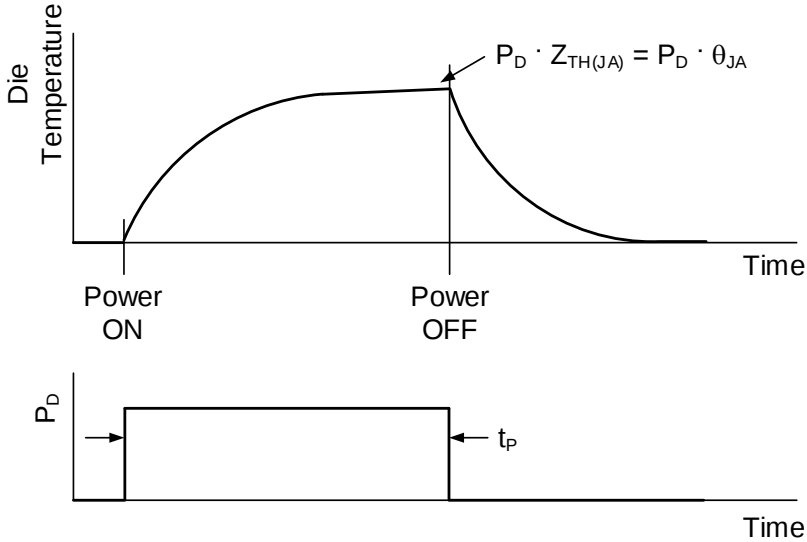
# How to use Zth to calculate the Tj

## Zth Curve

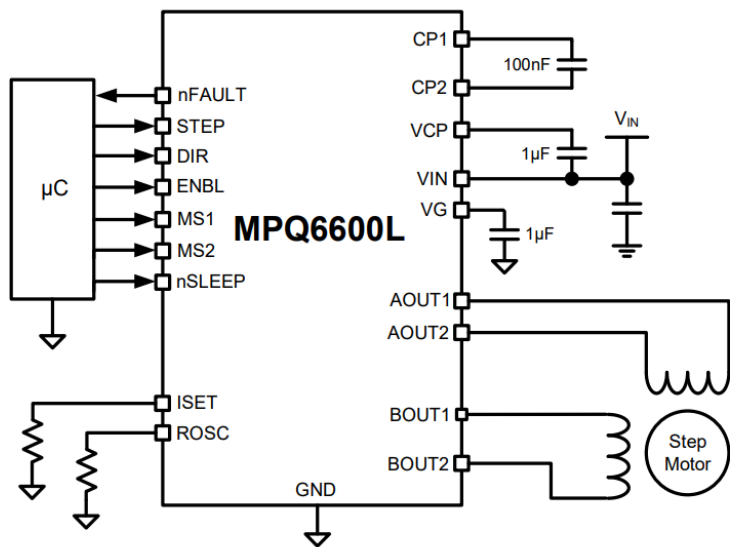


## Transient calculation related

$$T_J = P_D \times Z_{th}$$



# How to use Zth to calculate the Tj (Cont'd)

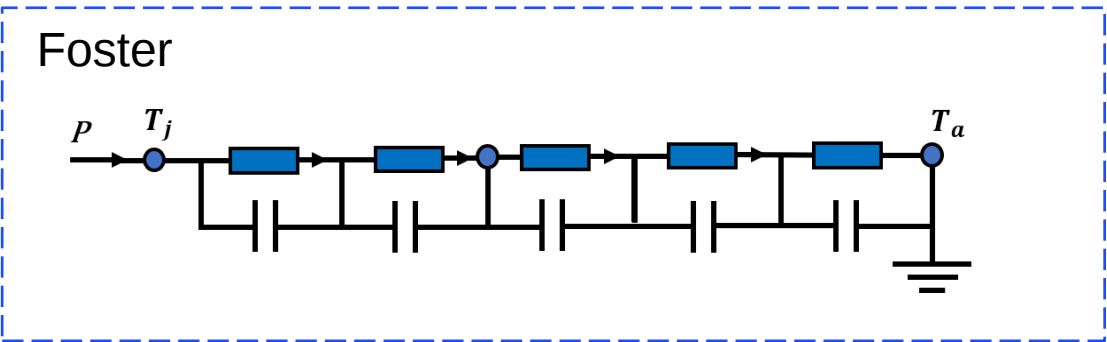


$$Z_{th}(t) = \sum_{i=1}^n r_i \left(1 - e^{-\frac{t}{\tau_i}}\right)$$

$$\tau_i = r_i C_i$$

## Background

1. Based on EVQ6600L-R-00A
2. Assumed that even heat is spread on each FETs



|         |              |         |                |
|---------|--------------|---------|----------------|
| Cth1 /F | 6.348760E-01 | Rth1 /Ω | 1.46521000E-03 |
| Cth2 /F | 6.158431E+00 | Rth2 /Ω | 1.27947204E-01 |
| Cth3 /F | 8.166576E+00 | Rth3 /Ω | 1.93982226E+01 |
| Cth4 /F | 1.740248E+00 | Rth4 /Ω | 3.27211250E-02 |
| Cth5 /F | 5.968462E+00 | Rth5 /Ω | 2.27979106E+01 |
| Cth6 /F | 3.840516E+00 | Rth6 /Ω | 1.78817714E+00 |
| Cth7 /F | 1.405920E-01 | Rth7 /Ω | 4.43541000E-04 |

# How to use Zth to calculate the Tj (Cont'd)

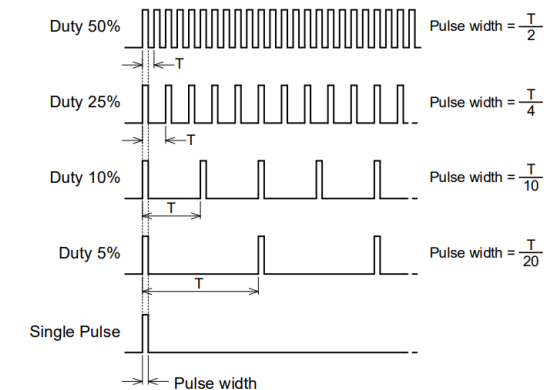
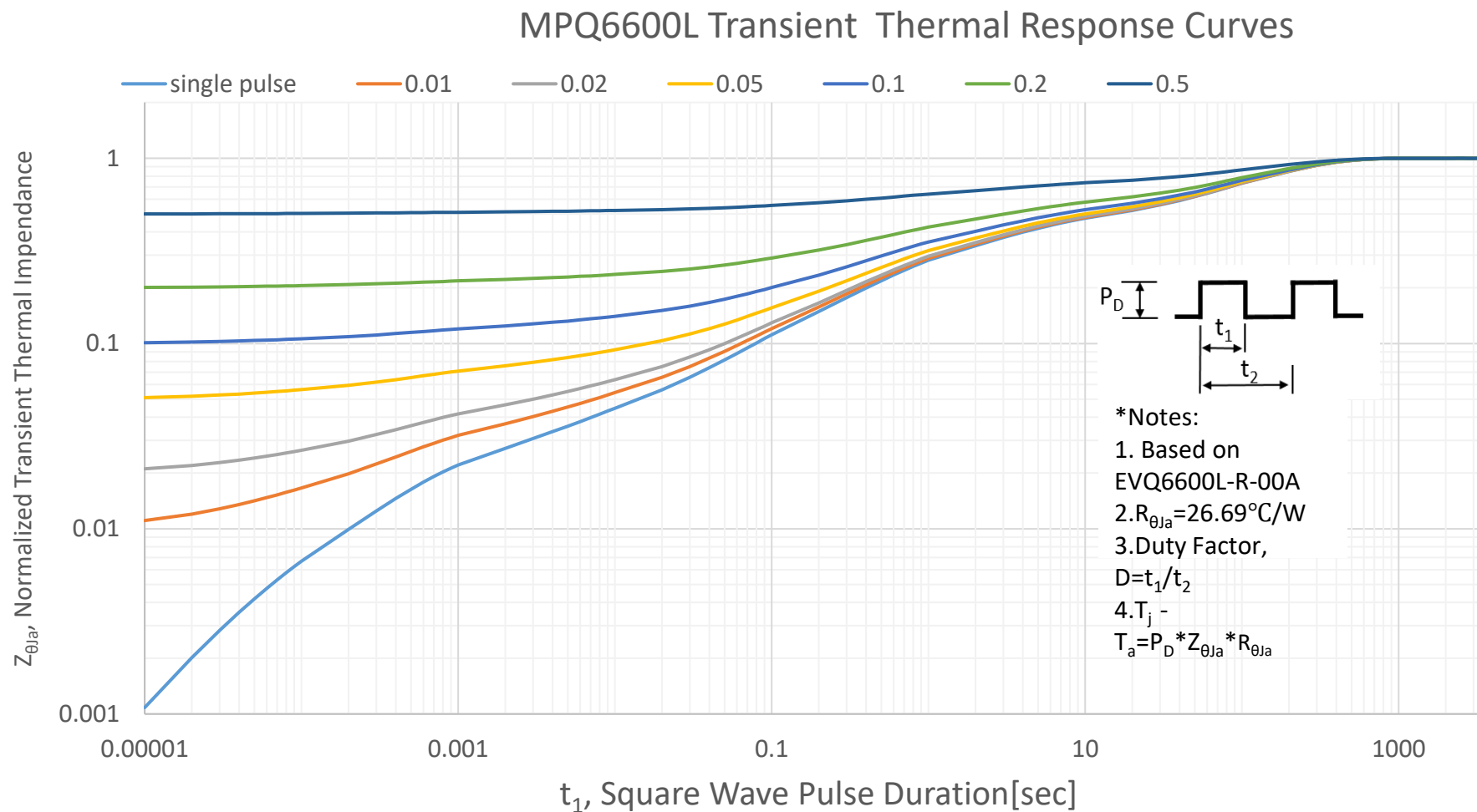
```
import matplotlib.pyplot as plt
from math import e
import numpy as np
```

```
R_th = [6.34876e-1,6.158431e+0,8.166576e+0,1.740248e+0,5.968462e+0,3.840516e+0,1.40592e-1]
C_th = [1.46521e-3,1.27947204e-1,1.939822263e+1,3.2721125e-2,2.279791058e+1,1.788177141e+0,4.43541e-4]
```

```
assert len(R_th) == len(C_th)
```

```
th = len(R_th)
#x = np.arange(0,1,0.0001,dtype = float)
x = np.logspace(-6, 0, num=7, base=10) # 对数域
y= np.sum([R_th[i] * (1-e**(-1*x/(R_th[i]*C_th[i]))) for i in range(th)],axis=0) # Foster模型的热阻抗曲线方程
plt.figure(figsize=(25,9))
plt.yscale("log") # 对数坐标
plt.xscale("log") # 对数坐标
plt.xlim(1E-6,1)
plt.ylim(1E-3,1)
# 开启刻度线网格
plt.grid(which='major',axis='both',linewidth=0.75,linestyle='-',color='orange')
plt.grid(which='minor',axis='both',linewidth=0.25,linestyle='-',color='orange')
plt.plot(x,y)
plt.show()
```

# How to use Zth to calculate the Tj (Cont'd)



1. The X-axis is Pulse width, representing the time power is applied to the device.
2. The Y-axis is the value of the transient thermal resistance.
3. The Y curve set is transient thermal resistance data.
4. The differences among the curves in the curve cluster are due to the varying duty cycles of the applied pulse power. Figure 2 shows the waveforms of pulse width and duty cycle used during measurement.

# How to use Zth to calculate the Tj (Cont'd)

## How to use it?

Step 1. Observe the power pulse width and duty cycle applied to the power devices and record the values.



Step 2. Read the transient thermal resistance values from the chart.



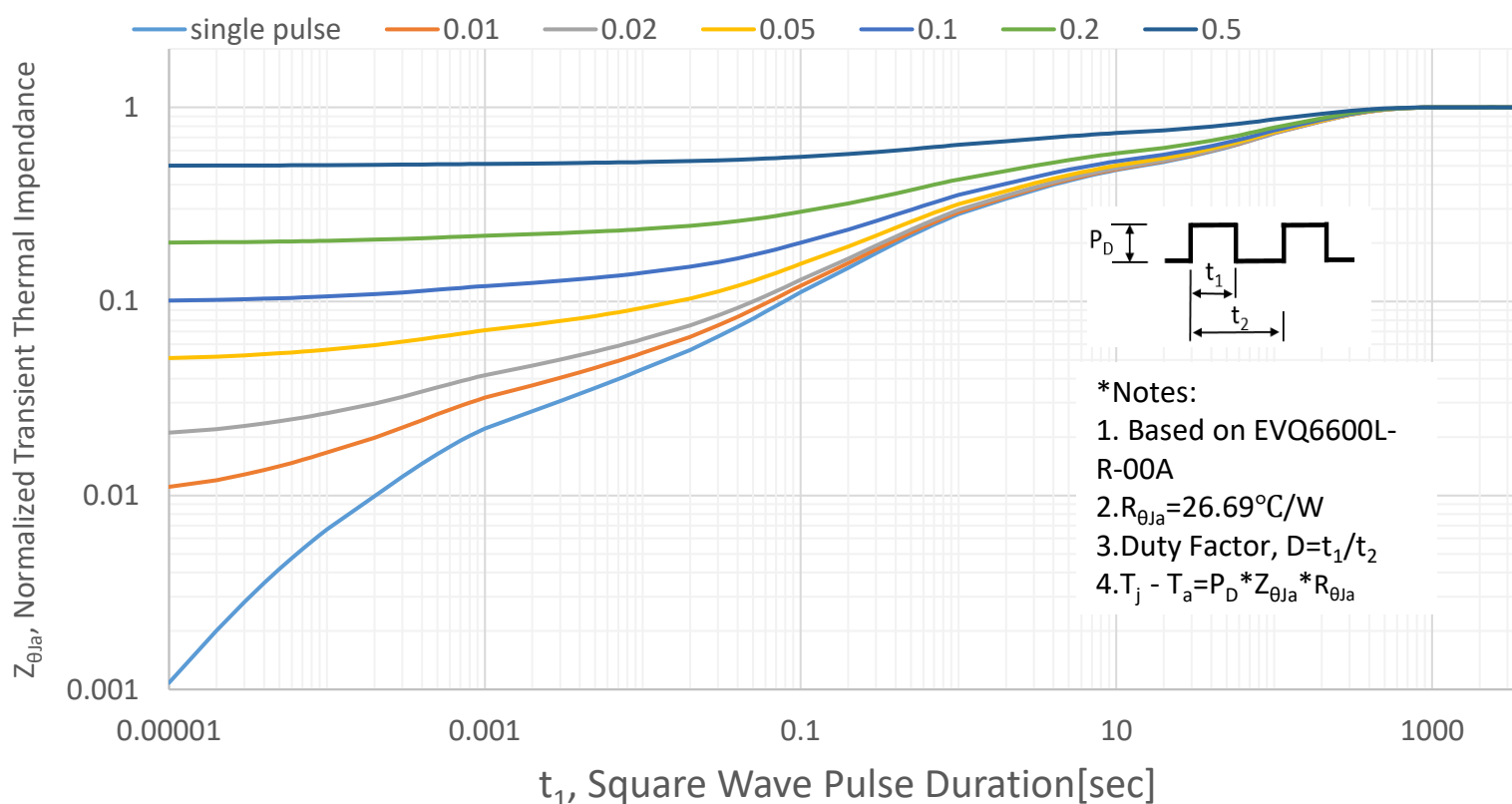
Step 3. Calculate the power loss of IC



Step 4. Calculate the junction temperature by the formula.

$$T_J = T_A + Z_{TH} \times P \text{ [}^\circ\text{C]}$$

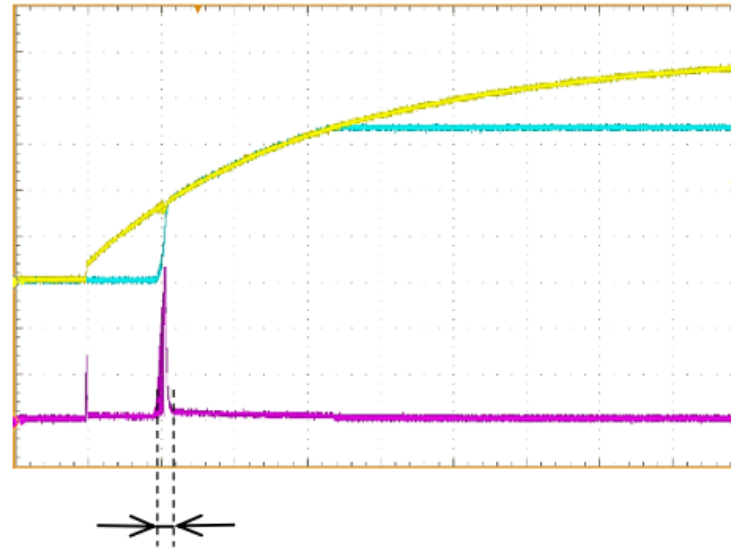
MPQ6600L Transient Thermal Response Curves



# Example one---Single Pulse

## Background

During the circuit startup, phenomena such as surge currents may often occur, which happen only for a short time. Therefore, the [Single Pulse] curve is used to estimate the junction temperature.

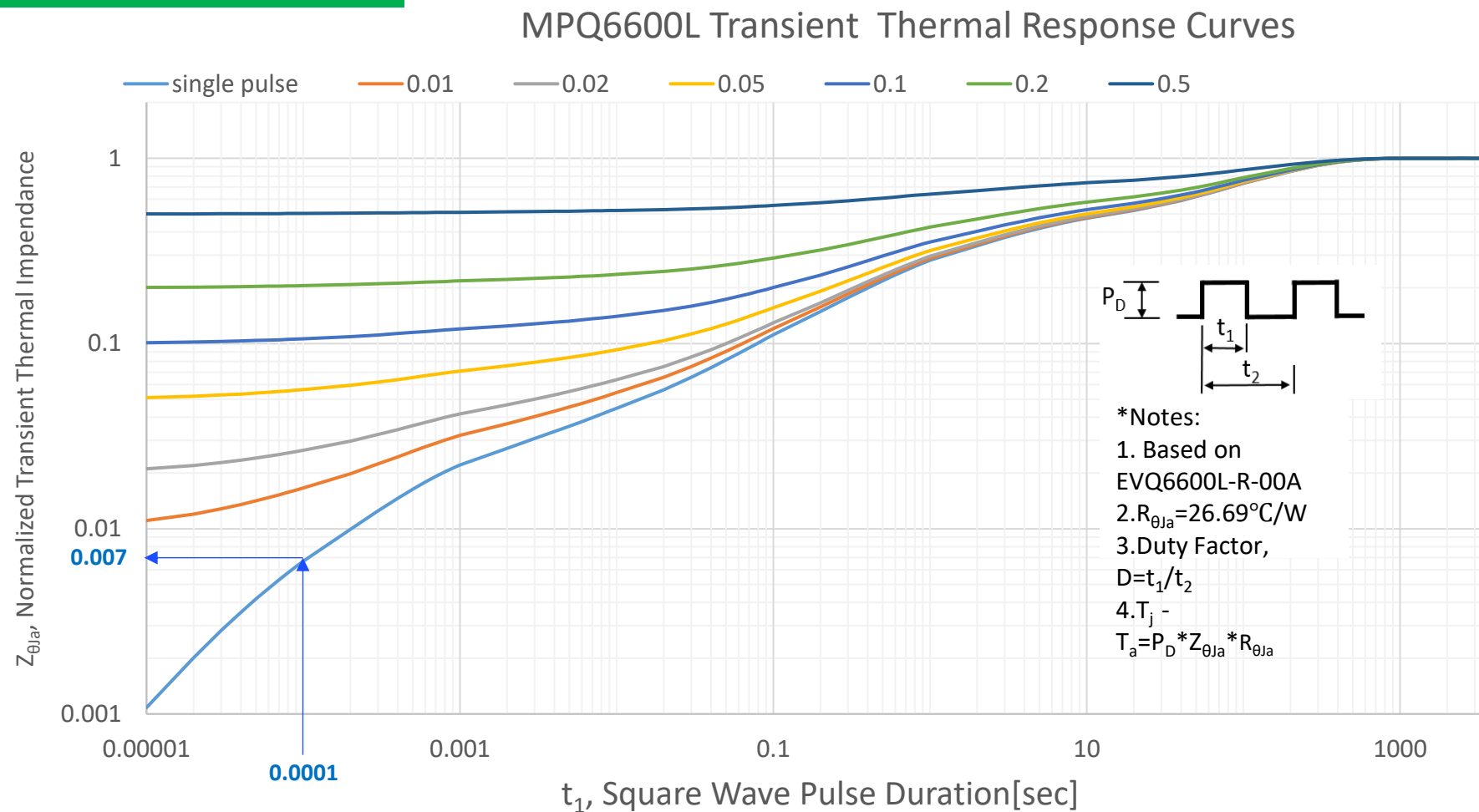


## Setp1

Pulse width is measured about **0.1ms**.

# Example one. (Cont'd)

## Setp2: Find the Zth



## Example one. (Cont'd)

### Setp3: The calculation

Calculate the junction temperature by the formula.

$$T_J = T_A + Z_{TH} \times P \text{ [}^\circ\text{C]}$$

$T_A$ : The ambient temperature



**60°C**

$Z_{TH}$ : the transient resistance from junction to ambient



**(0.07\*26.69=1.8683) °C/W**

$P$ : Power loss



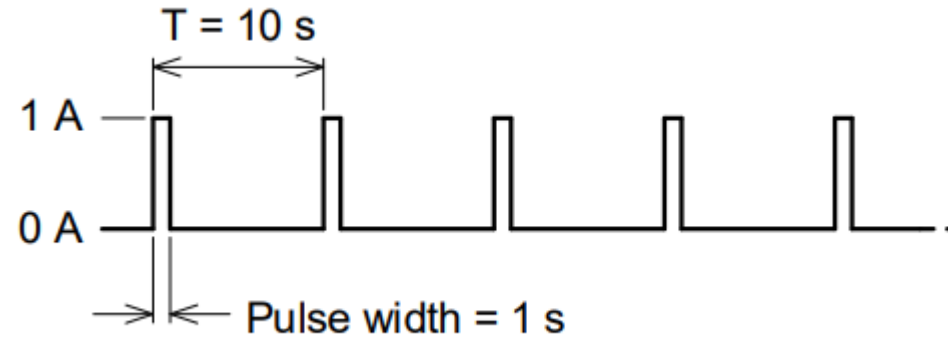
**10W**

$$T_J = 60 + 1.8683 * 10 = 78.683 ^\circ$$

## Example Two---Duty xx%

### Background

During the circuit is working under on-off mode, use the Duty curve to do the calculation of junction temperature

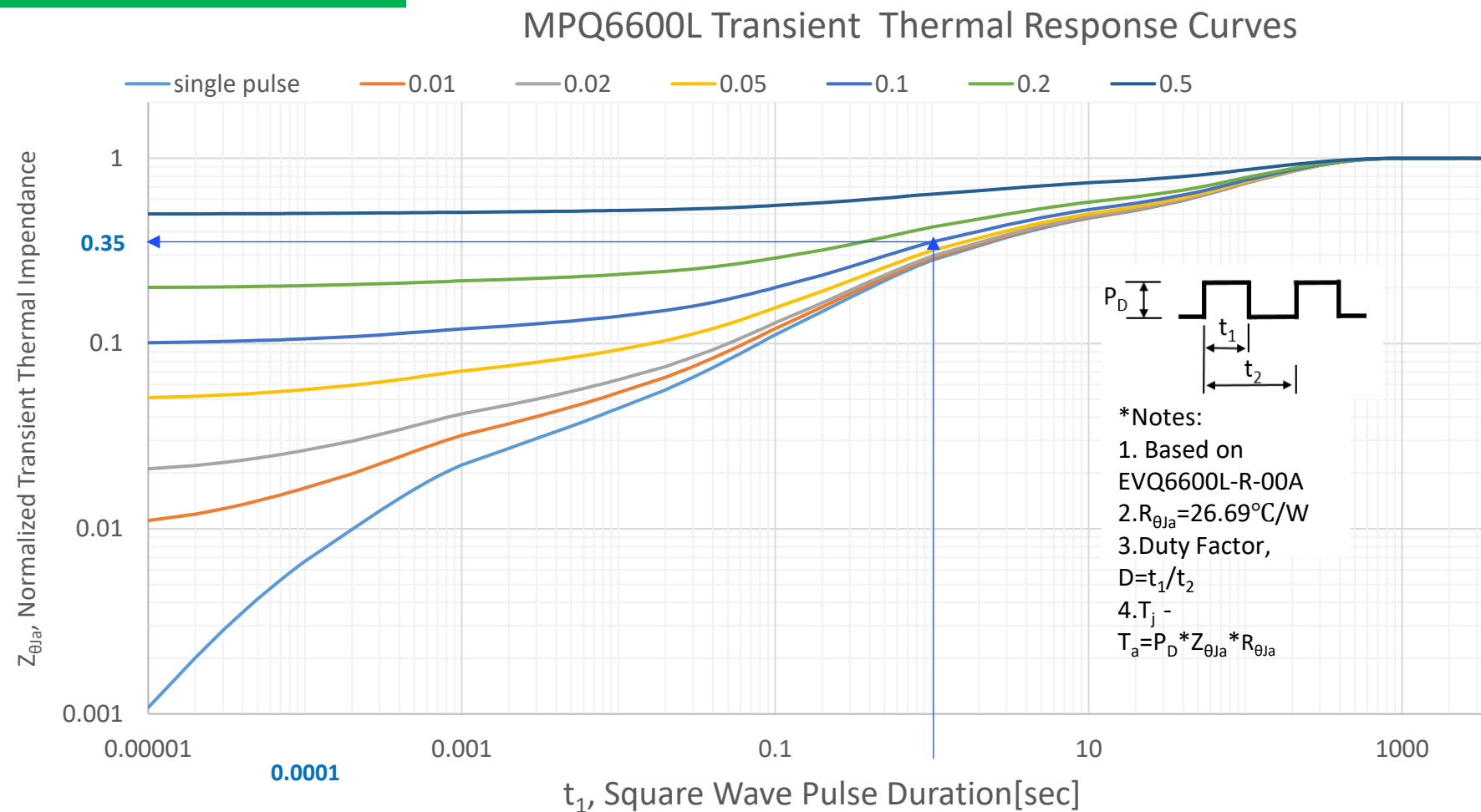


### Setp1

Pulse width is measured about **1s**, **10%Duty**.

# Example two. (Cont'd)

## Setp2: Find the Zth



## Example two. (Cont'd)

### Setp3: The calculation

Calculate the junction temperature by the formula.

$$T_J = T_A + Z_{TH} \times P \text{ [}^\circ\text{C]}$$

$T_A$ : The ambient temperature



**50°C**

$Z_{TH}$ : the transient resistance from junction to ambient



**(0.35\*26.69=9.3415) °/W**

$P$ : Power loss



**2W**

$$T_J = 50 + 9.3415 * 2 = 68.683^\circ$$

# Conclusion

- Power loss calculation: Switching loss and Conduction loss
- $C_{gd}$ ,  $C_{gs}$
- How to use thermal Resistance Parameters
- Pulsed operation, Cauer, Foster,  $Z_{th}$
- How to use  $Z_{th}$ ?

**Thank you for watching**